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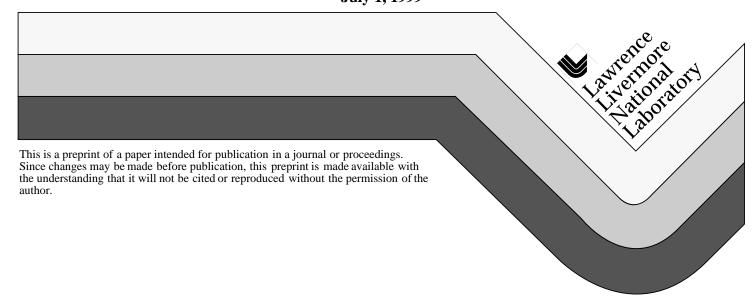
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Modeling short-pulse-driven collisional X-ray lasers and other new schemes

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ABSTRACT

Recently, the technique of using a nsec pulse to preform and ionize the plasma followed by a psec pulse to heat the plasma has enabled low-Z neon-like and nickel-like ions to lase driven by small lasers with only ten joules of energy. In this work we model recent experiments done using the COMET laser at LLNL to illuminate 1 cm long slab targets of Ti with a 4.8 J, 800 ps prepulse followed 1.6 nsec later by a 6 J, 1 psec drive pulse. The LASNEX code is used to calculate the hydrodynamic evolution of the plasma and provide the temperatures and densities to the XRASER code, which then does the kinetics calculations to determine the gain. The temporal and spatial evolution of the plasma is studied both with and without radiation transport included for the 3d and 3s _ 2p Ne-like Ti resonance lines. Large regions with gains greater than 80 cm ⁻¹ are predicted for the 3p ${}^{1}S_{0}$ __3s ${}^{1}P_{1}$ Ne-like Ti laser line at 326 Å. Given the large gain and large gradients in these plasmas, we do propagation calculations including refraction to understand which regions have the right combination of high gain and low gradients to contribute to the X-ray laser output. Calculations are also presented using different delays between the long and short pulse and different widths for the short pulse to provide better insight for optimizing the laser output. In addition to the standard 326 Å laser line, high gain is also predicted and observed for the 3d ¹P₁ – 3p ¹P₁ laser line at 301 Å in Ne-like Ti. We present calculations with and without radiation transport included on the strong $3d^{-1}P_{1} = 2p^{-1}S_{0}$ resonance line to better understand this self photopumping effect. We also look at the analog transition in Ni-like ions to understand if self photopumping may also play a role in Ni-like ions. High gain is predicted on the 3d9 4f ¹P₁ _ 3d ⁹ 4d ¹P₁ Ni-like transition and this line has recently been observed at 226 Å in Ni-like Mo. Gain of 13 cm⁻¹ has been measured for this line.

Keywords: X-ray laser, multiple pulse technique

1. INTRODUCTION

Most researchers today use some variant of the prepulse or multiple pulse technique [1-3] to achieve lasing in Ne-like or Ni-like ions. As a result the Ne-like 3p ¹S₀ __3s ¹P₁ laser line now dominates the laser output as was predicted two decades ago. These techniques illuminate solid targets with several pulses. The first pulse is used to create a large scale length plasma which is in the correct density range for gain and has sufficiently small density gradients for laser propagation. The subsequent pulses are then absorbed more efficiently and heat the plasma to lasing conditions. Typical pulse durations are 100 ps for the multiple pulse technique and up to 1 ns for the prepulse technique and typically use 100 to 1000 J of energy. In the above techniques the pulse duration is held constant but the contrast and separation between pulses is varied. A recent variant of these techniques, which has now become very common, is the use of a nsec prepulse followed by a psec drive pulse. This approach was first used to demonstrate lasing at 326 Å in Ne-like Ti at the Max Born Institute (MBI) [4] using less than 10 joules of energy. The Ti experiments were reproduced at Lawrence Livermore National Laboratory (LLNL) using the COMET laser and extended to Ni-like Pd at 146 Å [5]and very recently to Ni-like Mo at 189 Å [6]. In this paper we model the Ne-like Ti experiments done with the COMET laser to understand the plasma conditions present and what gain is possible on different transitions. In addition to the Ne-like Ti 3p ¹S₀ __3s ¹P₁ transition at 326 Å we discuss the photopumping mechanism [7,8] which drives the gain of the Ne-like Ti 3d ¹P₁ __3p ¹P₁ transition at 301 Å. For Ni-like Mo we present lasing on both the 4d ¹S₀ _ 4p ¹P₁ line at 189 Å and the 4f ¹P₁ _ 4d ¹P₁ line at 226 Å. For the 4f ¹P₁ _ 4d ¹P₁

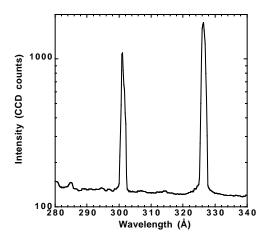


Fig. 1. Ne-like Ti spectrum showing lasing at 301 and 326 Å.

line we discuss the role of the photopumping mechanism and present measured gain of 13 cm⁻¹ for the 226 Å Ni-like Mo line. We also present the calculated and measured wavelengths for the 4f $^{1}P_{1-}$ 4d $^{1}P_{1}$ line for Z from 36 to 54.

2. PLASMA MODELING OF NE-LIKE TI EXPERIMENTS

To model the Ti experiments done at the COMET facility we did LASNEX one dimensional (1D) computer simulations of a Ti slab illuminated by a 4.8 J, 800 psec gaussian pulse followed 1.6 nsec later by a 6 J, 1 psec gaussian pulse from a $1.05 \text{ }\mu\text{m}$ Nd laser. The laser is focused to a $50 \text{ }\mu\text{m}$ wide by 1.2 cm long line. The 1.6 nsec delay between the long and short pulse is peak to peak. This is similar to the conditions used to demonstrate lasing in Ne-like Ti and Ni-like Pd at the COMET laser

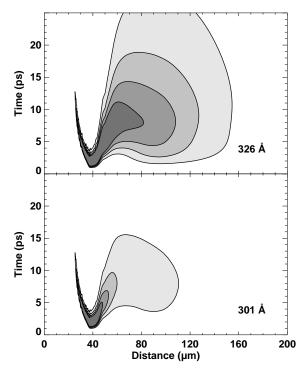


Fig. 2. Gain for the Ne-like Ti laser lines versus space and time. The short pulse laser drive peaks at 1 ps on the time axis. Contours represent gain > 80, 60, 40, and 20 cm⁻¹.

facility. The LASNEX calculations include an expansion angle of 15 degrees in the dimension perpendicular to the primary expansion so as to simulate 2D effects.

The LASNEX calculated densities and temperatures are used as input to the XRASER code, which calculates the gains of the laser lines including radiation trapping effects for the four strong 3d and $3p_2$ 2p resonance lines in Ne-like Ti. Bulk Doppler effects due to the expansion of the plasmas were also included. The Ti atomic model used by the XRASER code includes all 89 detailed levels for levels up to n = 4 in Ne-like Ti.

Four dominant laser lines are predicted and these can be divided into two classes. The 3p 1S_0 ___3s 1P_1 line at 326 Å and the 3p 1S_0 ___3s 3P_1 line at 285 Å share the same upper laser level which is populated by monopole collisional excitation of the Ne-like ground state. The 285 Å line typically has half the gain of the 326 Å line because its oscillator strength is smaller by a factor of 2. The second set of lines are the 3d 1P_1 ___3p 1P_1 line at 301 Å and the 3d 1P_1 ___3p 3P_1 line at 314 Å. These lines share the same upper laser state which is populated primarily by photopumping on the strong 2p 1S_0 ___3d 1P_1 transition. Both lines are predicted to lase, with the gain on the 314 Å line about 25% lower because of its weaker oscillator strength. In experiments done at MBI and LLNL only the stronger monopole collisional and photopumped lines at 326 and 301 Å lines are observed and we will only discuss those two lines further in this paper. Figure 1 shows a laser spectrum taken during an experiment at the COMET laser. One observes strong lasing on both the 326 and 301 Å laser lines. While the 326 Å line is very robust to changes in laser conditions the intensity of the 301 Å line is quite sensitive to small changes and its intensity varies a lot from shot to shot.

Figure 2 shows contours of the gain versus space and time for the 326 Å and 301 Å laser lines for the nominal drive conditions described above. The short pulse laser peaks at 1 psec on this time scale so the evolution during the long pulse is not shown. The horizontal axis gives the distance from the target surface in the direction of the plasma expansion. The gain contours represent gains greater than 80, 60, 40, and 20 cm⁻¹. The highest gain for the 326 Å line exceeds 200 cm⁻¹ at 40 µm, which is near the critical density surface, just after the time of peak illumination, 2 psec. This gain region is very small and short lived and has steep gradients which would make it difficult to propagate any significant distance. If one looks at the 2nd

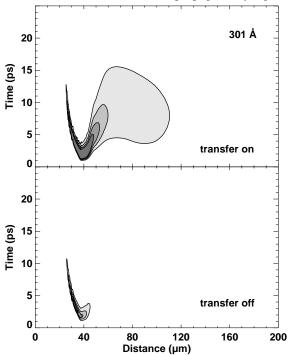


Fig. 3. Gain of the Ne-like Ti 301 Å laser line with line transfer turned on and off versus space and time. The contours represent gain > 80, 60, 40, and 20 cm⁻¹.

gain contour with g > 60 cm⁻¹ one can see that this region of large gain peaks about 80 μ m from the target surface at about 8 psec, which is long after the short pulse laser has turned off. The gain lasts about 10 psec and extends over 50 μ m. For the 301 Å laser line the gain region is somewhat shorter lived and has a smaller spatial extent which helps explain why this line is more sensitive to small changes in the experimental conditions. For both lines there is also a very narrow gain region which follows the critical density surface but that region is unlikely to allow laser propagation over any significant distance.

Normally, we would not expect gain on the 301 Å line because its upper laser state is the 3d $^{1}P_{1}$ level, which is depopulated by the rapid radiative decay to the ground state via the strongest resonance line. In this plasma, however, the 2p $^{1}S_{0}$ __3d $^{1}P_{1}$ line is optically thick and radiation trapping allows a very large radiation field to build up on this line and populate the 3d $^{1}P_{1}$ upper laser state by the photopumping process (radiative excitation). To understand this mechanism, we did the XRASER calculations with the line transfer package turned off so that all the n = 2 _ n = 3 resonance lines are optically thin and the self photopumping process is absent. For the 326 Å laser line, looking 80 µm from the surface at 9 ps, there is a modest reduction of one-third in the gain. For the 301 Å laser line, Fig. 3 shows contours of the gain with line transfer on and off. In contrast to the 326 Å laser line, the gain of the 301 Å laser line disappears without the photopumping process except for a very small region near the critical density surface.

We can better understand the role of the photopumping process by comparing the collisional and radiative rates from the Ne-like ground state to the 3d $^{1}P_{1}$ upper laser state versus distance from the target surface at 8.9 psec, as shown in Fig. 4. At 80 µm from the surface the radiative rate is more than an order of magnitude larger than the collisonal excitation rate. The collisional rate falls very rapidly with the electron density while the radiative rate depends on the photon density. While collisional excitations create the photons, the large optical depth of the 2p $^{1}S_{0}$ __3d $^{1}P_{1}$ line, _ = 300, allows photons which are created in the hot dense plasma near the surface and throughout the plasma to be trapped and contribute to the photopumping process.

One of the important parameters which affects the X-ray laser performance is the delay between the long and short pulse. Figure 5 shows the gain contours versus space and time for three different values of the delay, 0.6, 1.6, and 2.6 nsec. For the shortest delay of 0.6 nsec the gain has a small temporal and spatial extent near the critical density surface just after the time of peak laser illumination. Given the large gradients in the plasma one would not expect to see any significant lasing in this case. For the longest delay of 2.6 nsec, the gain duration is much longer but has a narrow spatial extent. In contrast, for the 1.6-nsec delay, the gain has both a large spatial and temporal extent. The electron density gradients are also smallest for the 1.6-nsec case, which allows the X-rays to propagate through the gain region and be amplified better. During the short pulse laser illumination the hydrodynamics does not change much and the main change in electron density is just due to ionization. For all three delays, the electron temperature becomes quite high, with peak values over 800 eV, so this is not a

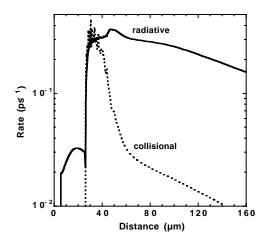


Fig. 4. Radiative and collisional rates for the $2p^{-1}S_0 \rightarrow 3d^{-1}P_1$ transition versus distance from the target surface at 8.9 ps show the photopumping process driving the gain for the 301 Å laser line.

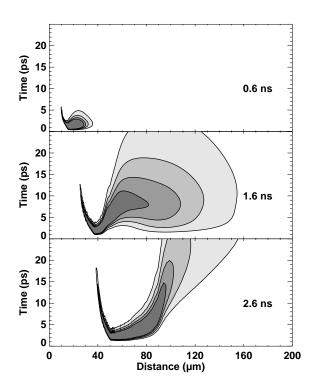


Fig. 5. Gain of the Ne-like Ti 326 Å laser line versus space and time for three values of the delay between the long and short pulses. The short pulse laser peaks at 1 ps on the time axis. Contours represent gain > 80, 60, 40, and 20 cm^{-1} .

limiting factor.

A big difference between the three cases is the ionization balance. Figure 6 shows the fraction of Ne-like Ti versus

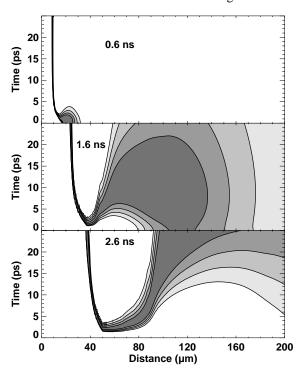


Fig. 6. Ne-like Ti ion fraction versus space and time for three values of the delay between the long and short pulses. Contours represent Ne-like fractions > 50, 40, 30, and 20%.

space and time for the three delays. Recall that the short pulse laser peaks at 1 psec on this time scale. The darkest contours represent Ne-like fraction greater than 50% with the other contours being 40, 30, and 20% fraction. For the 0.6-nsec delay the plasma tends to be overionized except at high densities. The long pulse over ionizes the plasma and the delay is too short to allow recombination to Ne-like. For the 2.6-nsec delay the plasma is underionized so that at time zero, before the short pulse laser is turned on, there is no Ne-like population except in the low-density region far from the gain region. In contrast, for the 1.6 nsec delay there is a large Ne-like population before the short pulse laser heats the plasma. It appears that the best delay is one that prepares the plasma with a large Ne-like population. The short pulse laser then can quickly heat the electrons, which drives the collisional excitation rate, without allowing time for the plasma to overionize.

For the optimum 1.6-nsec delay we also did calculations with different short pulse energy. If we double the short pulse energy to 12 J the gain increases and the region of high gain expands in time and space. Halving the energy to 3 J reduces the gain and shrinks the gain region. This is consistent with the general observation that hitting a target harder makes it lase better. Given the long time duration for the gain compared with the 1 ps drive laser we did a calculation where we kept the energy of the short pulse laser at 6 J but increased the pulse duration to 5 ps. In that case we observed similar gain to the 1 ps drive case but the time duration of the gain increases slightly and the spatial extent decreases slightly. This suggests that a longer drive pulse should work just fine and that energy on target is the more important issue since we are operating in a regime where the gain duration is longer than the pulse duration of the drive laser. The longer pulse would have the advantage of relaxing the requirements on implementing the traveling wave geometry in the experiments. For example the use of stepped mirrors or tilted compressor gratings to make the traveling wave geometry introduce non-ideal features that might be less of a problem with the use of the longer pulse drive.

To understand the effect of refraction on the X-ray laser output we return to the case of the optimum 1.6 nsec delay. To study the refraction issue we consider a 1 cm long plasma which we illuminate from the end by a source which is weighted by the upper level population of the laser transition. We then do a ray tracing calculation with amplification to determine the near field and far field laser intensity versus space and time. For simplicity we assume traveling wave illumination by the short pulse laser. The laser output peaks at 8 psec with a FWHM duration of 1 psec. This shows that the gain region, which is contributing most to the output, is near 8 psec. If we now integrate over time and look at the laser intensity versus source position we observe a peak about 90 μ m from the target surface. These X-rays start at 90 μ m from the surface but are pointed inwards about 10 mrad so that they sample gain even closer to the surface before they are refracted back out. If we look at the plasma 90 μ m from the surface at 8 psec the electron density is 8.2 x 10¹⁹ cm⁻³ with an electron density gradient of -6.5 x 10²¹ cm⁻⁴. A 326 Å photon propagating through down a 1 cm length with this gradient would be bent by 15 μ m. The refraction effect is quite small in this region, which no doubt accounts for why it contributes so much to the laser output.

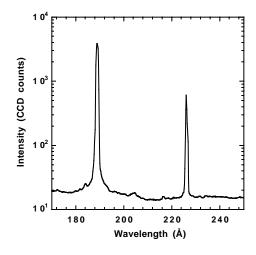


Fig. 7. Ni-like Mo spectrum showing lasing at 189 and 226 Å.

3. NI-LIKE MO EXPERIMENTS

We have also had great success making Ni-like ions lase under similar conditions as those used for the Ne-like Ti experiments at the COMET laser facility. In this section we will discuss our recent experiments on Ni-like Mo and in particular discuss the successful lasing observed on the 4f $^{1}P_{1}$ 4d $^{1}P_{1}$ photopumped line. To make Mo lase, we used a 600 FWHM pulse to preform and ionize the plasma followed by a 1 ps pulse to heat the plasma. The delay between the two pulses was 700 ps. A maximum energy of 5 joules was used in the short pulse and only 1 joule in the long pulse. The beams were focused to a 70 μ m \times 1.25 cm line on to the slab targets that vary in length up to 1 cm. The long pulse was defocused by a factor of 2 to ensure better overlap between the beams from the long and short pulse. A five-segmented stepped mirror was used to provide travelling wave illumination of the target at the speed of light.

Figure 7 shows an on-axis Mo spectrum with the strong $4d^{1}S_{0} \rightarrow 4p^{1}P_{1}$ line lasing at 189 Å and the weaker $4f^{1}P_{1} \rightarrow 4d^{1}P_{1}$ line lasing at 226 Å. The ratio between the lines is slightly distorted because the 189 Å line is saturated on the detector. However the 226 Å line lases very well and both lines completely dominate the background emission. Lasing on the 189 Å $4d^{1}S_{0} \rightarrow 4p^{1}P_{1}$ line in Ni-like Mo has been discussed in two recent papers [6,9] so we will not discuss this further here.

To measure the gain of the 226 Å line we did a length study by using polished Mo targets that varied in length from 0.2 to 0.9 cm. Figure 8 shows the intensity versus target length for this line from which we estimate a gain of 13 cm⁻¹. There is no sign of saturation in this figure. In our modeling we estimate the saturation intensity of the 226 Å line at 9 GW cm⁻² under the plasma conditions at the time of peak gain. This is almost three times the saturation intensity estimated for the 189 Å line and indicates that while the 226 Å line is weaker and has lower gain it does have the potential to be the stronger line.

We have also observed lasing on the $4f\,^1P_1 \rightarrow 4d\,^1P_1$ line in Ni-like Zr and Nb. The wavelengths of the measured laser lines with their uncertainties are given in Table 1. While this line has not been observed directly in nonlasing plasmas, its wavelength can be calculated by using the measured values of the 3d $^1S_0 = 4f ^{-1}P_1$ resonance line together with the experimentally determined values for the energy of the $4d\,^1P_1$ lower laser state. This approach is described in Ref. 10 and the experimentally based wavelengths for Z = 37 to 42 are given in Table 1 along with their uncertainties. For Z = 40 to 42 these values agree with the values measured in the X-ray laser experiments within the experimental uncertainties. The maximum disagreement is $0.7\,\text{Å}$.

We calculated the wavelengths of the laser lines using the multi-configuration Dirac-Fock (MCDF) atomic physics code of Grant et al. in the extended average level (EAL) mode doing separate calculations for the J=1 even and odd parity states. The energies of the 4f $^{1}P_{1}$ and 4d $^{1}P_{1}$ level were subtracted to calculate the energy of the laser transition. We fit the difference between the energies calculated by the MCDF code and the experimentally determined energies for Z=37 to 42 to a straight line and then subtracted this curve from the MCDF calculation. For Z=42 the correction was 0.77 eV. The wavelengths

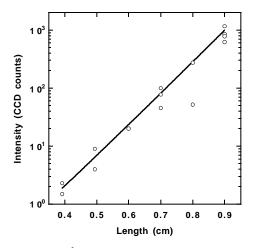


Fig. 8. Intensity versus length for the 226 $\hbox{\AA}$ Ni-like Mo photopumped laser line. Measured gain is 13 cm $^{-1}$.

Table 1. Wavelengths in Å of the 4f $^{1}P_{1} \rightarrow 4d$ $^{1}P_{1}$ transition in Ni-like ions. Uncertainty of the last digit is given in parentheses.

Z	Laser measurement	Calculated from experimental energies	Predicted wavelengths
36		,	443.4
37		383.9(2)	383.6
38		337.1(2)	337.3
39		300.4(2)	300.6
40	271.0(2)	270.8(3)	270.9
41	246.4(3)	247.0(5)	246.5
42	226.0(3)	226.7(5)	226.1
43			208.9
44			194.1
45			181.3
46			170.1
47			160.4
48			151.8
49			144.7
50			135.5
51			129.6
52			124.0
53			118.8
54			114.0

predicted by this method are given in Table 1 for Z=36 to 54. We believe these values are accurate to better than 1 Å. Similar calculations done for the 4d $^{1}S_{0} \rightarrow 4p$ $^{1}P_{1}$ line are described in Ref. 9.

To understand the photopumping process we modeled the Mo plasma using the LASNEX and XRASER codes as described above for Ti. In the calculations, the gain of the 226 Å laser line peaks about 1 ps after the peak of the short pulse at 27 μ m from the target surface with a peak gain of 160 cm⁻¹. The very high gain falls by half within 2 ps but gain greater than 20 cm⁻¹ persists for 8 ps after the short pulse. In Fig. 9 we show rates typical for the plasma at 5 ps after the peak of the short pulse at 50 μ m from the target surface. The radiative excitation rate due to photopumping is the dominant rate and is an order of magnitude larger than the collisional excitation rate which is populating the 4f upper laser level. The optical depth of the 3d 1 S₀ $_{-}$ 4f 1 P₁ resonance line is 100 and the line strength is 0.0163 photons per mode. The gain of the 226 Å Mo line is 37 cm⁻¹ with an electron temperature of 295 eV, an ion temperature of 47 eV, ion density of 4.42 x 10¹⁸ cm⁻³ and an electron density of 6.30 x 10¹⁹ cm⁻³. The gain profile has a spatial FWHM width of 60 μ m. The gradient in the electron density is -1.69×10^{22} cm⁻⁴. For a 226 Å X-ray, this gradient would refract the X-ray by only 19 μ m over a 1-cm propagation length. The collision rates shown for the lower laser state are net rates out of the level. In the absence of photopumping the gain disappears and goes slightly negative.

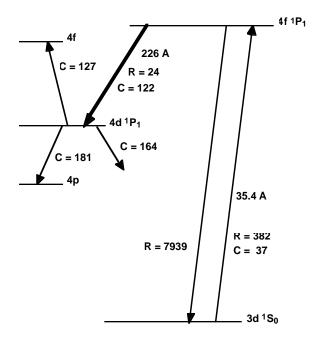


Fig. 9. Energy level diagram showing the collisional (C) and radiative (R) rates ($nsec^{-1}$) which drive the 226 Å Ni-like Mo $4f^{\,1}P_{1} \rightarrow 4d^{\,1}P_{1}$ X-ray laser line. Lasing is driven by the strong photopumping from the 3d $^{\,1}S_{0}$ ground state to the $4f^{\,1}P_{1}$ upper laser level.

4. CONCLUSIONS

In this work we model recent experiments done using the COMET laser at LLNL to illuminate 1 cm long slab targets of Ti with a 4.8 J, 800 ps prepulse followed 1.6 nsec later by a 6 J, 1 psec drive pulse. The LASNEX code is used to calculate the hydrodynamic evolution of the plasma and provide the temperatures and densities to the XRASER code, which then does the kinetics calculations to determine the gain. The temporal and spatial evolution of the plasma is studied both with and without radiation transport included for the 3d and 3s _ 2p Ne-like Ti resonance lines. Large regions with gain greater than 80 cm^{-1} are predicted for the 3p $^{1}\text{S}_{0}$ __3s $^{1}\text{P}_{1}$ Ne-like Ti laser line at 326 Å. Given the large gain and large gradients in these plasmas, we do propagation calculations including refraction to understand which regions have the right combination of high gain and low gradients to contribute to the X-ray laser output. Calculations are also presented using different delays between the long and short pulse and different widths for the short pulse to provide better insight for optimizing the laser output. The delay appears to play a large role in preparing the plasma in the correct ionization stage prior to the short pulse heating the plasma. In addition to the standard 326 Å laser line, high gain is also predicted and observed for the 3d $^{1}\text{P}_{1}$ _ 3p $^{1}\text{P}_{1}$ laser line at 301 Å in Ne-like Ti. We present calculations with and without radiation transport included on the strong 3d $^{1}\text{P}_{1}$ _ 2p $^{-1}\text{S}_{0}$ resonance line to better understand this self-photopumping effect.

For Ni-like Mo we demonstrate lasing on both the 4d $^{1}S_{0}$ _ 4p $^{1}P_{1}$ line at 189 Å and the 4f $^{1}P_{1}$ _ 4d $^{1}P_{1}$ line at 226 Å. For the 4f $^{1}P_{1}$ _ 4d $^{1}P_{1}$ line we explain how the photopumping mechanism drives the gain of this line and present measured gain of 13 cm⁻¹ for this line. We also present the calculated and measured wavelengths for the 4f $^{1}P_{1}$ _ 4d $^{1}P_{1}$ line for Z from 36 to 54.

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